FIELD THEORY

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(lecture notes prepared by Ejnar Gyldenkerne)

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TO MY GIRLS
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PREFACE

In the fall of 1979, Benny Lautrup and I set out to write the ultimate Quantum Chromodynamics review. The report was going to consist of four parts, one for each line of

From Ghoulies and Ghosties
and Long-leggety Beasties
and Things that go bump in the Night
Good Lord, deliver us!

Ghoulies are body-snatchers and grave robbers; they are those revel in that which is revolting.

Benny had previously described ghosties in a very nice set of QCD lectures† which we were going to use as the first part. Green functions resemble long-leggety beasties; they, and the general formalism of field theory, were to be developed in the second part. The things that go bump in the night are clearly the many unpleasant surprises of field theory; divergences, together with the regularization and computation techniques, were to be covered in the third part. Finally, good Lord deliver us, we were going to actually calculate a few basic QCD integrals.

Well, while I was lecturing about the long-leggety beasties, Benny deserted me for lattice, and the ultimate QCD review was never written. That these lectures appear at all is largely due to tireless work by Ejnar Gyldenkerne and to the criticisms of the QCD study group at the Niels Bohr Institute. In writing these lectures I have profited much from discussions with Benny Lautrup, to whom I direct my thanks.

Critics say:

... Seen in [Cvitanović's] framework, field theory books are like every other form in the universe: they are generated by changing intervals of tension between a dominant system and a competing system in a space-time continuum that is dependent on the process of competition between these two stabilities and not on any General Concept of Space and Time ... [Cvitanović's] method thus valorizes the microcosm which illuminates macrocosmic form by the high tendency of microcosmic patterns to repeat themselves and so greatly limit structural variation in the macrocosm ... But on another level, as in the sagas, the Song of Rolland, the Illiad, the Odyssey, the Nibelungenlied, the Aeneid and Beowulf, the real dynamic focus of the book is the power of anger.

Patricia Harris Stablein

A distinguished reviewer says:

IT IS NOT EVEN WRONG